# Timing Vulnerabilities in Phasor Measurement Units

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Electrical and Computer Engineering

## **Phasor Measurement Units**

### "MRI of The Power System"

Power Grid Corporation of India Limited, on Schweitzer Engineering Laboratory's Synchrophasor System

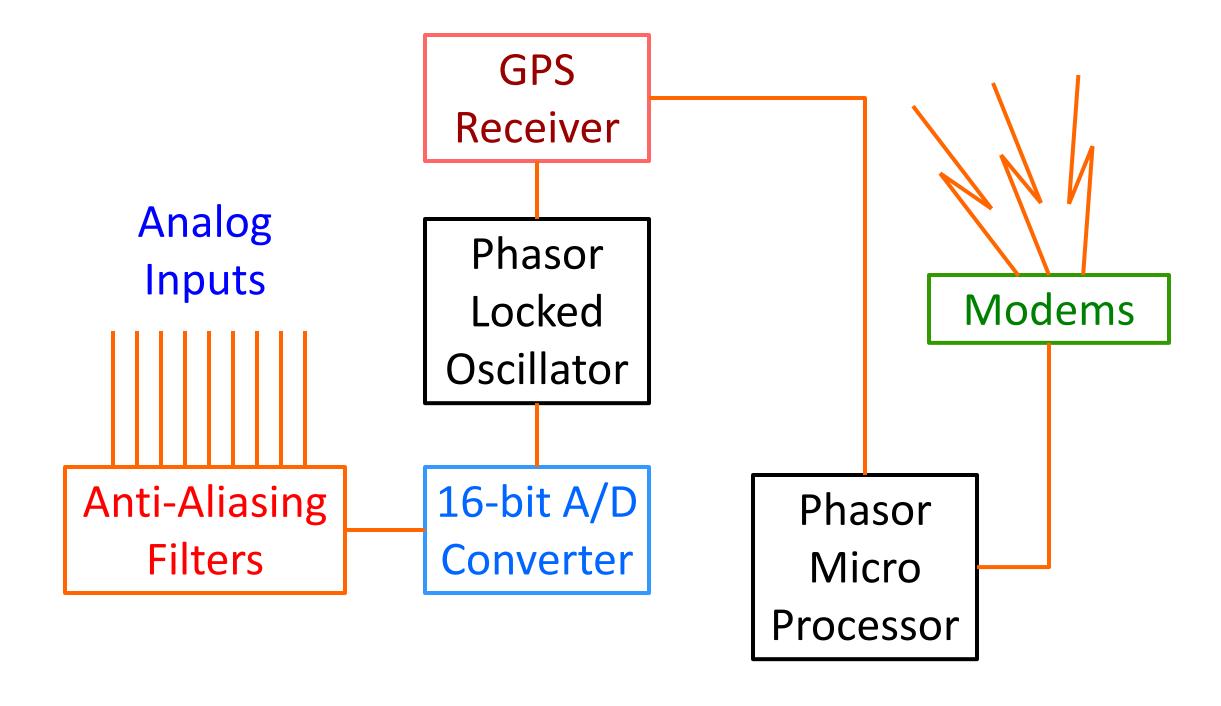
### Synchrophasors

- Voltage and current phasors measured synchronously at widely dispersed locations on power grid
- Can be compared in real time
- Improve upon traditional state estimation, calculated using unsynchronized data points collected every 2-4 seconds
- Can be used to provide a comprehensive dynamic overview of the system state in real-time, assess state of electrical system and manage power quality

#### Phasor Measurement Units

- Invented in 1988 at Virginia Polytechnic Institute and State University, by Dr. Arun G. Phadke and Dr. James S. Thorp
- Output precisely time-stamped Synchrophasors
- One of the most important measuring devices in the future of power systems
- Used for:
  - Wide-area monitoring and control
  - High-precision state estimation
  - Forensic event analysis
  - Adaptive load shedding
- Synchrophasor system consists of Phasor Data Concentrators (PDCs) which collect data from several PMUs and communicate to the Supervisory Control and Data Acquisition (SCADA) system.

# PMU Block Diagram



(Adapted from R.F. Nuqui, "State Estimation and Voltage Security Monitoring Using Synchronized Phasor Measurements", Doctorate Dissertation, Virginia Polytechnic Institute, Blacksburg, VA, July 2, 2001.)

# **Global Positioning System**

#### **Accuracy Requirements**

- For 60 Hz systems, PMUs must deliver between 10 and 30 synchronous reports per second depending on the application
- Accuracy of ±0.5 μS necessary for synchrophasor measurement
- Global Positioning System (GPS) provides necessary accuracy along with synchronization among geographically distant PMUs and PDCs

#### Vulnerability

- PMUs are protected against loss of GPS signal, unintentional or otherwise use internal reference clock for several seconds
- GPS broadcasts can be spoofed without jamming
- Practicality of GPS spoofing established by the work of Prof.
  Brumley et al, Carnegie Mellon University
- Attack involves fabricating a counterfeit signal from a GPS satellite, placing an antenna to ensure fake signal drowns out real one
- A properly orchestrated attack will change time-stamps on PMU measurements, causing a phase difference in State Estimation (SE)

### State Estimation Defense

- Bad Data Detection removes false measurements prior to SE
- Attack can only be successful if Bad Data Detection is evaded

# Linear Analysis

#### Assumption

- Measurements are linear functions of state
- Lines are reactive lossless and only reactive
- Voltage magnitudes are 1 pu only phases need to be estimated
- Current injections at both ends of branch are equal and opposite
- Voltage phase differences are small

#### Extent of Disruption

- Measurement Function: y = f(x), Jacobian:  $H = \frac{\partial y}{\partial x}$
- State Estimation:  $\hat{\mathbf{x}} = (\mathbf{H}^T \mathbf{R}^{-1} \mathbf{H})^{-1} \mathbf{H}^T \mathbf{R}^{-1} \mathbf{z}$
- Measurement Estimation:  $\hat{z} = Hx = H(H^TR^{-1}H)^{-1}H^TR^{-1}z = Kz$
- Residues (used for BDD):  $\mathbf{r} = \mathbf{z} \hat{\mathbf{z}} = (\mathbf{I} \mathbf{K})\mathbf{z}^{\kappa}$
- Attacker wants to add attack vector a to measurements z attack will fail if a is in null space of (I-K)
- All column vectors of  $\mathbf{H}$  are in the null space of  $(\mathbf{I} \mathbf{K})$  any linear combination of the columns is a valid attack vector
- Convex/Non-Convex Optimization gives desired attack vector

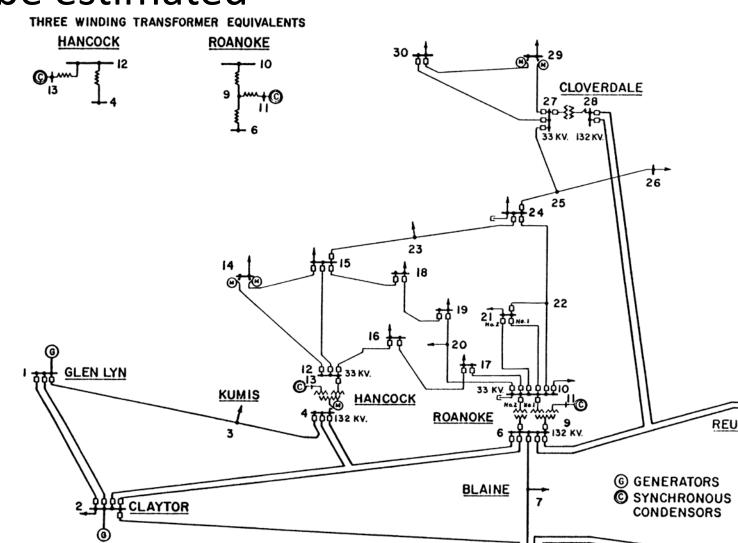
# Non-linear System

#### **\*** Failure of Linear Assumptions

- Lines are lossy, measurements are non-linear functions of state
- Unequal current injections increase possible measurements
- Voltage magnitudes must be estimated
- Systems are complex
- IEEE 30-bus system
- Shown in figure

• 30 Buses

- 41 Branches
- 59 States
- 224 Measurements



## Simulation Results

### System Assumptions — IEEE 30 Bus System

- PMU on 10 out of 30 buses measure
  - Bus voltage magnitudes and phases
  - Current magnitudes and phases for all connected branches

### Attacker Assumptions

Changes time on Bus 27 PMU by 6 μS

#### Observations

- Without attack, 0 bad data,  $\Delta V = 6 \times 10^{-5}$  pu,  $\Delta \varphi = 2 \times 10^{-3}$ ° (max)
- Under attack, 3 bad data,  $\Delta V=0.014$  pu,  $\Delta \varphi=0.3^{\circ}$  (max)
- Max. change in active power estimate: 0.024 pu, 28%
- Max. change in reactive power estimate: 0.0700 pu, 104%

# Conclusions & Future Work

### **Effect of PMU Timing Attacks**

- Attack on 1 PMU out of 10 can cause significant estimation error
- Estimation of active/reactive power can change widely, can cause:
  - Change Adaptive Load-Shedding Strategy
  - Change in Control Strategy
  - Change in Electricity Pricing

#### Future Work

- Theoretically estimate disruptions
- Optimize attack vector maximum damage, minimum detectability
- Perform hardware-in-the-loop simulations
- Improve detection scheme to prevent timing attacks

