



# Computing Locational Contingency Reserves

-Simulation and DyMonDs application  
to Bulk Power System Reliability-

Jose Fernando Prada

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# Managing uncertainty is a key challenge of future smart grids

- ❖ Forced outages are an important source of uncertainty in bulk power systems operation
  - Generating units and transmission lines
  - Impact reliability and security of operations
- ❖ Reliability standards seek to prevent it
  - N-1 criterion: requires the system to withstand the loss of one major component without interruption

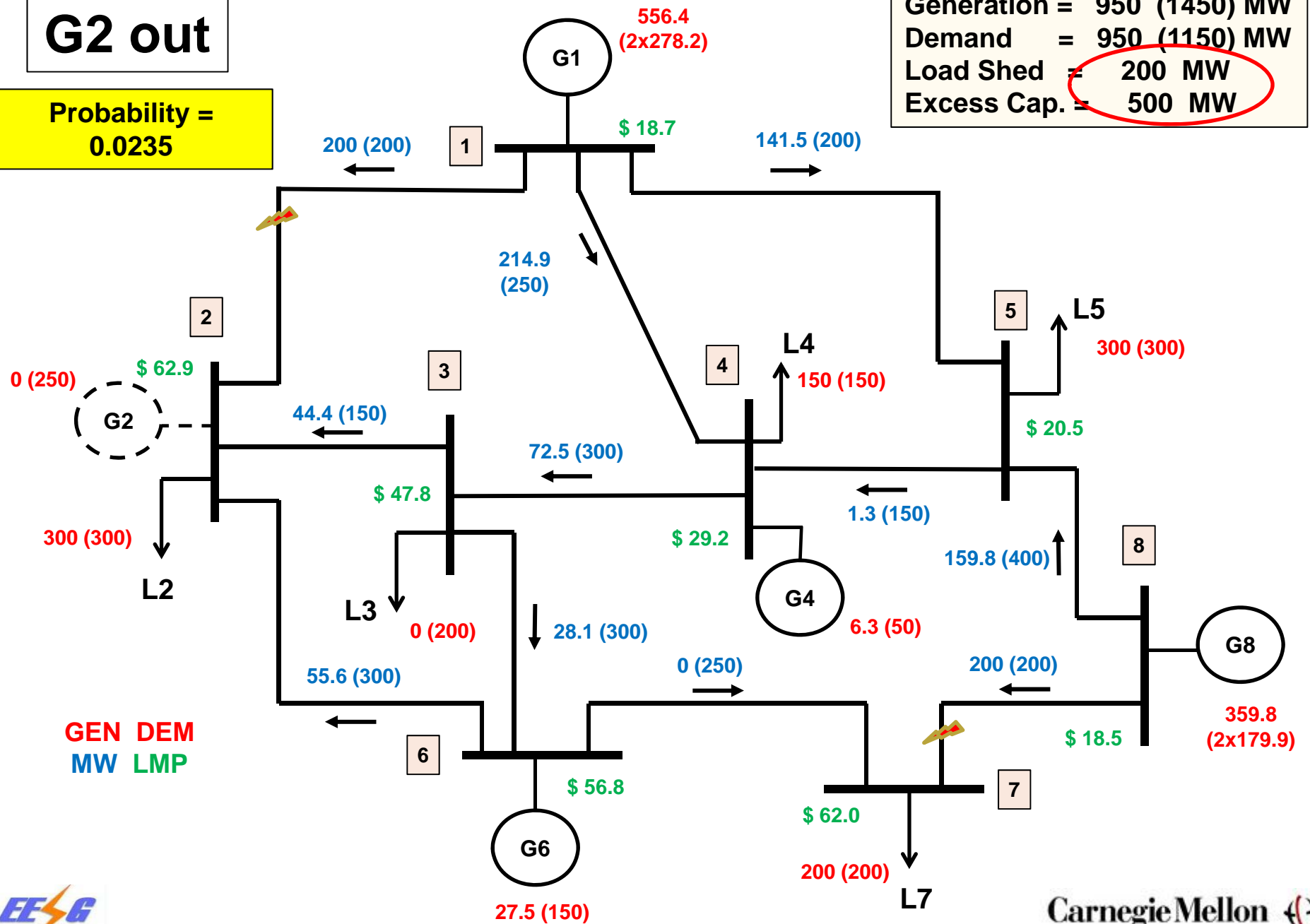
# But the traditional approach to operational security is insufficient

- ❖ Spare capacity is reserved to provide for generation outages
- ❖ The reserve requirement is a fixed amount
  - Equivalent to losing the biggest generator online and/or some percentage of expected demand.
- ❖ This contingency reserve may not be deliverable when a contingency occurs
  - Due to transmission constraints in the network
  - As a result, N-1 is weakly enforced or costly manual adjustments are required

**G2 out**

Probability =  
0.0235

Generation = 950 (1450) MW  
Demand = 950 (1150) MW  
Load Shed = 200 MW  
Excess Cap. = 500 MW



# A different approach to allocate contingency reserves is needed

- ❖ Abandon the traditional reserve requirement
  - Lack of technical basis for a fixed requirement
- ❖ Identify required locational contingency reserves
  - To fully satisfy N-1 criterion, taking into account all credible generation outages
- ❖ Conceptual approach:
  - Co-optimize expected cost of energy plus cost of providing reserves, considering credible outages

# Stochastic SCUC for energy and reserves

$$\min_{x_{it}, u_{it}, g_{it}^{(0),(k)}} \sum_{i \in G} \sum_{t \in T} \sum_{k \in K} \left[ S_i x_{it} + w^{(0)} C_i \left( g_{it}^{(0)}, u_{it} \right) + O_{it}(r_{it}) + w^{(k)} C_i \left( g_{it}^{(k)}, u_{it} \right) \right]$$

$$\sum_{i \in G_n} g_{it}^{(0)} + \sum_{p \in P_n} B_{pn}^{(l)} \theta_{pn,t}^{(l)} = D_{nt} ; \quad \forall n, \forall t, \forall l$$

$$\sum_{i \in G_n} g_{it}^{(k)} + \sum_{p \in P_n} B_{pn}^{(k)} \theta_{pn,t}^{(k)} = D_{nt} ; \quad \forall n, \forall t, \forall k$$

$l$  : index of line contingencies

$k$  : index of generation contingencies, 0 when normal state

$O_i$  : cost of reserves provided by unit  $i$

$w$  : contingency probability

Nodal power balances (DCPF) w/ unit contingencies

$$r_{jt} = \max[g_j^{(k)} - g_{jt}^{(0)}]^+, \quad \forall j \in G_{fast}, \forall t$$

$$RD_j \leq g_{jt}^{(k)} - g_{jt}^{(0)} \leq RU_j ; \quad \forall j \in G_{fast}, \forall t$$

$$RD_i \leq g_{i,t} - g_{i,t-1} \leq RU_i ; \quad \forall i, \forall t$$

$$-T_{pn,t} \leq B_{np}^{(k,l)} \theta_{np,t}^{(k,l)} \leq T_{np,t} ; \quad \forall np, \forall k,l, \forall t$$

$$x_{it} + u_{i,t-1} \geq u_{i,t}$$

$$R_t = \sum r_{jt}$$

No previously fixed reserve requirement

# Practical solution: decompose the problem in two deterministic stages

- ❖ Proposed formulation achieves a better allocation of contingency reserves, but the stochastic SCUC problem is hard to solve.
- ❖ Separate the problem into a centralized UC (1<sup>st</sup> stage) and co-optimization of energy and reserves (2<sup>nd</sup> stage)
  - Both are deterministic
  - In second stage simulate credible (single) unit outages to identify needed reserves

# Network constrained economic dispatch (2nd stage)

For each period  $t$ , minimize energy and reserve costs **across all  $k$  contingencies**:

$$\min_{g_{it}^{(k)}, r_{it}^{(k)}} \sum_i [C_i(g_{it}^{(k)}) + O_i(r_{it}^{(k)})] ; \quad (7)$$

Subject to:

$$\sum_{i \in N_n} g_{it}^{(k)} + \sum_{p \in P_n} B_{pn} \cdot \theta_{jn,t}^{(k)} = D_{nt} ; \quad \forall n, \forall t, \forall k \quad (8)$$

$$g_{it}^{(k)} = g_{it}^{(0)} ; \quad \forall i \neq s \quad (9)$$

$$g_i^{\min} \leq g_{it}^{(k)} \leq g_i^{\max} ; \quad \forall i, \forall t, \forall k \quad (10)$$

$$RD_s \leq g_{st}^{(k)} - g_{st}^{(0)} \leq RU_s ; \quad \forall s, \forall t \quad (11)$$

$$r_{it}^{(k)} = \max[0, (g_{it}^{(k)} - g_{it}^{(0)})] , \quad \forall i=s \quad (12)$$

$$-T_{pn,t} \leq B_{np} \cdot \theta_{np,t}^{(k)} \leq T_{np,t} ; \quad \forall p, \forall n, \forall k, \forall t \quad (13)$$



# NCED can be solved in a decentralized way using DyMonDs approach

❖ To facilitate computation and processing

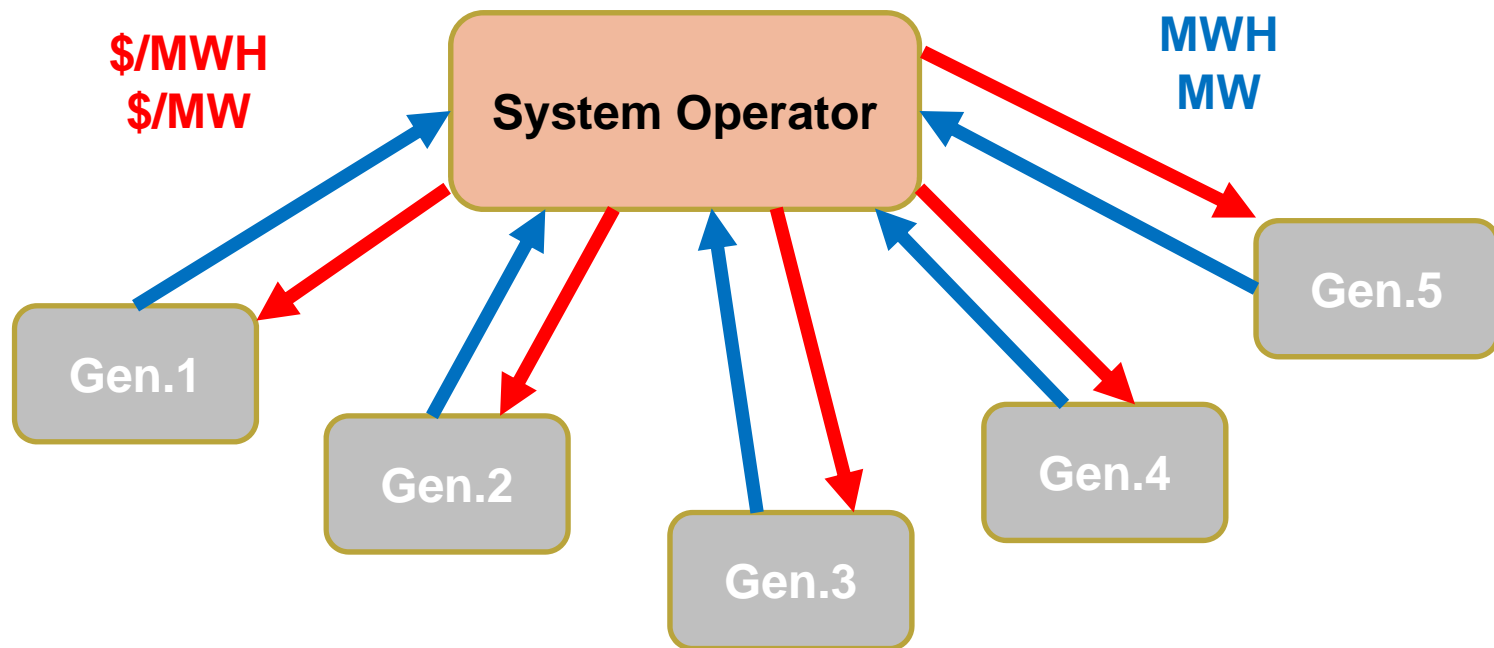
❖ DYMONDS approach

- Replace centralized problem solution by system operator (SO)
- Let generators optimize energy and reserve bids, based on prices posted by the system operator
- Solution within the time framework of Real-Time markets

# Locational reserves with DyMonDS

- ❖ System operator posts estimated energy and reserve prices
- ❖ Generators optimize energy and reserve bids subject to posted prices
  - Max. profit, incorporating generation constraints
- ❖ SO receives and clears the bids and compute a new set of energy and reserve prices.
- ❖ The process is iterated until all problem constraints are met.

# Simulation of decentralized NCED



**Energy and Reserve Prices**

**Energy and Reserve Bids**

# Solution can be simulated in a small test system with DyMonDS

- ❖ To prove feasibility of approach
- ❖ To measure convergence time
- ❖ To establish communication requirements
- ❖ To verify protocols for information exchange
- ❖ To verify quality of the solution

# Thank you

[jfprada@andrew.cmu.edu](mailto:jfprada@andrew.cmu.edu)

