## Transactive Control: A Novel Technology for Smart Grids

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## Outline

• A Smart Grid – A Paradigm Shift

- Transactive Control
  - Dynamic Market Mechanisms
  - Integrated Secondary and Primary Control
- Case Studies





### Paradigm Shift: From Current to Smart Grids



## Smart Grid Control

- To maintain power balance in the system.
- To ensure that operating limits are maintained
  - Generators limit
  - Tie-lines limit
- To ensure that the system frequency is constant (at 50 Hz or 60Hz).
- To achieve the above with renewable energy despite intermittency & uncertainty
- To ensure affordable power







### THE OVERALL VISION



Vision for Smart Grid Control: 2030 and Beyond: Reference Model and Roadmap (Eds. M. Amin, A.M. Annaswamy, C. DeMarco, and T. Samad), IEEE Standards Publication, November 2013.



## **Distributed Decision and Control**

- Primary control
  - Immediate (automatic) action to sudden change of load.
  - For example, reaction to frequency change.
- Secondary control
  - Restore system frequency,
  - Restore tie-line capacities to the scheduled value, and,
  - Make the areas absorb their own load.
- Tertiary control
  - Make sure that the units are scheduled in the most economical way.





### Transactive control: An Emerging Paradigm\*

The use of dynamic market mechanism to send an incentive signal and receive a feedback signal within the power system's node structure

- Incentive Signal: Dynamic Pricing
- Feedback Signal: Adjustable Demand

\* Hammerstorm et al., "Standardization of a Hierarchical Transactive Control System"





## Transactive Control: Example

- Pacific Northwest
   Demonstration Project
- 112 Households participating in 2009

3 min 30 s

- 60,000 households in an ongoing project (2010-2015)
- Spans several states

15 s

1:35 pm



Courtesy of Olympic Peninsula Project, IBM TIS: Transactive Incentive Signal

#### TFS: Transactive Feedback Signal

## Transactive control: Our Definition

The use of dynamic market mechanism to send an incentive signal and receive a feedback signal within the power system's node structure

- Incentive Signal: Ex. Dynamic Pricing
- Feedback Signal:
  - Adjustable Demand (Market Level)
    - (Price Responsive, and Regulation Responsive)
  - Area Control Error (Secondary Level)
  - Governor Control (Primary Level)

#### Transactive Control — Control architecture that coordinates

- Market Transactions
- Active Control at the AGC level with Regulation Demand Response



### **Transactive Control Framework\***



\* A. Kiani, A.M. Annaswamy, and T. Samad, "A Hierarchical Transactive Control Architecture for Renewables Integration in Smart Grids." HYCON Workshop, Brussels, 2012.

### **Primary Level**

$$\begin{bmatrix} \dot{x}_{G} \\ \dot{x}_{L} \\ \varepsilon \dot{P}_{G} \\ \varepsilon \dot{P}_{L} \end{bmatrix} = \begin{bmatrix} A_{G} & 0 & -c_{G} & 0 \\ 0 & A_{L} & 0 & c_{L} \\ Y_{GG}E_{G} & Y_{GL} & -I & 0 \\ Y_{LG}E_{L} & Y_{LL} & 0 & -I \end{bmatrix} \begin{bmatrix} x_{G} \\ x_{L} \\ P_{G} \\ P_{L} \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ \phi_{G} \\ \phi_{L} \end{bmatrix} + \begin{bmatrix} b_{G} & 0 \\ 0 & b_{L} \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \omega_{ref} \\ P_{L}^{ref} \\ 0 \\ 0 \end{bmatrix} + \begin{bmatrix} \Delta_{G} \\ \Delta_{L} \\ 0 \\ 0 \end{bmatrix}$$

- time scale t



## Secondary Level

$$0 = Ax_{p_{ss}}[k] + Bz_{p_{ss}}[k] + Fu[k] + D_{p_{ss}}$$
  

$$0 = Cx_{p_{ss}}[k] + Dz_{p_{ss}}[k] + f_{p_{ss}}[k] + Df_{p_{ss}}$$
  

$$\beta$$
  

$$x_{s}[k+1] = x_{s}[k] + B_{s}u_{s}[k] + C_{s}D_{s}[k]$$
  

$$x_{s}[k]: W_{G_{ss}} \quad u_{s}[k]: u[k+1] - u[k]$$

#### $\mathsf{D}_{s}[k]$ : Uncertainty in generation, load, and tie-line flow

Goal:  $x_s \rightarrow x_t$  a reference signal set by the tertiary level



$$e_s = \chi_s - \chi_t$$
: Area Control Error (ACE)  
Anuradha Annaswamy, Transactive Control



## **Tertiary Level**



How do we design the Tertiary Level?





## **Electricity Market**

- Centralized mechanism that facilitates trading of energy between buyers and sellers.
- The market operator conducts an auction market and schedules generators based on bids received.
- Determines a market clearing price (Locational Marginal Price (LMP)) and provides commitments and schedules based on security-constrained unit commitments



## Wholesale Market: A Dynamic System



## Market Mechanisms - LMP







### Top Layer: A Dynamic Market Mechanism



- 1. Equilibrium under constant flux.
- 2. GenCos and ConCos adjust their power level using a recursive process.
- **3**. Price is a Public Signal that guides all entities to adjust efficiently.

## **Modeling of Generating Company**

- ρ: market price ~ Locational Marginal Price at market equilibrium.
- The cost function of each generators unit is

$$C(P_{g_i}) = b_{g_i} P_{g_i} + \frac{c_{g_i}}{2} P_{g_i}^2$$



A dynamic model, for suppler i = 1, ..., M can be shown as

$$P_{g_{i_{k+1}}} = P_{g_{i_k}} + k_{p_{g_i}} (\rho_{n(i)_k} - c_{g_i} P_{g_{i_k}} - b_{g_i})$$

That is, if a generator observes a market price  $\rho_{n(i)_k}$  above the marginal cost  $c_{g_i}P_{g_{i_k}} + b_{g_i}$  will expand production until the marginal cost of production equals the price.





## **Modeling of Consumers Company**

- $P_{n(i)_k} = c_{d_j} P_{d_{j_k}} + b_{d_j}$ : marginal benefit of  $P_{d_j}$
- Consumer utility function:

$$U(P_{d_j}) = b_{d_j} P_{d_j} + \frac{c_{d_j}}{2} P_{d_j}^2$$



A dynamic model, for consumer j = 1, ..., N can be shown as

$$P_{d_{j_{k+1}}} = P_{d_{j_k}} + k_{P_{d_j}} (c_{d_j} P_{d_{j_k}} + b_{d_j} - \rho_{n(j)_k})$$

i.e. Demand  $P_{d_j}$  with a marginal benefit above the marginal price will lead to an expansion in consumption until equilibrium is attained.



## **Pricing Strategy**

• Energy imbalance  $E_k$  at time k

$$E_{k} = \left( -\sum_{i \in \theta} P_{g_{i_{k}}} + \sum_{j \in \theta} P_{d_{j_{k}}} + \sum_{m \in \Omega_{n}} B_{nm} \left[ \delta_{n} - \delta_{m} \right] \right)$$

• The pricing policy should depend on the degree of energy imbalance

$$\rho_{n_{k+1}} = \rho_{n_k} + k_\rho E_k$$





## A Dynamic Market Model

- The market participants need not have global market information.
- Convergence of the dynamic system to the equilibrium condition implies that the market reaches the condition of Nash equilibrium.



$$\begin{array}{l} \min f(x) \\ \text{s.t} \\ g(x) = 0 \\ h(x) < P \end{array} \xrightarrow{\text{Distributed}} \begin{array}{l} x_i(K+1) = \overline{x}_i(K) - hk_x \nabla_x L(\overline{x}_i(K), \overline{\rho}_i(K), \overline{\mu}_i(K)) \\ \varphi_i(K+1) = \overline{\rho}_i(K) - hk_\rho \nabla_\rho L(\overline{x}_i(K), \overline{\rho}_i(K), \overline{\mu}_i(K)) \\ \mu_i(K+1) = \overline{\mu}_i(K) - hk_\mu \left[ \nabla_x L(\overline{x}_i(K), \overline{\rho}_i(K), \overline{\mu}_i(K)) \right]_{\mu}^+ \end{array}$$

### Dynamic Market Mechanism (contd.)

The overall dynamic model:

$$X_{t}[K+1] = (I_{n} + hA)X_{t}[K] + hk_{\rho}\Delta + b$$

$$x_{t} = [\{P_{G}\}_{i} \ \{P_{D}\}_{j} \ \{\delta\}_{n} \ \{\rho\}_{n}]_{(n)\times 1}^{T}$$

$$A = \begin{bmatrix} -k_{g}c_{g} & 0 & 0 & k_{g}A_{g}^{T} \\ 0 & k_{d}c_{d} & 0 & -k_{d}A_{d}^{T} \\ 0 & 0 & 0 & k_{\delta}Y^{T} \\ -k_{\rho}A_{g} & k_{\rho}A_{d} & k_{\rho}Y & 0 \end{bmatrix}$$

 $n: N_g + N_d + 2N - 1$   $N_g: #GenCo N_d: #ConCo N: #buses$  $k_g, k_d, k_\delta, k_\rho$ : Parameters of the RTM dynamic model

- Quantifies effect of volatility and stability
- Can help reduce reserve costs with wind uncertainty 24 Anuradha Annaswamy, Transactive Control

### Interconnections



$$\sum_{PRI} : \begin{cases} \dot{x}_{p} = (A + E_{p})x_{p}(t) + Bz_{p}(t) + Fu[k] \\ \varepsilon \dot{z}_{p} = Cx_{p}(t) + Dz_{p}(t) + \phi_{p}(t) \end{cases}$$

$$\sum_{SEC} : x_{s}[k+1] = (\tilde{A}_{s} + C_{s}E_{s})x_{s}[k] + B_{s}L_{t}x_{t}[K] \\ \sum_{TER} : x_{t}[K+1] = \tilde{A}_{t}x_{t}[K] + hk_{p}E_{t}e_{s}[K] + b \\ e_{s}[k+1] = x_{s}[k+1] - R_{t}x_{t}[K]$$

 $x_{p} = \begin{bmatrix} \omega_{G} \\ \vdots \end{bmatrix}$  $x_{s} = \begin{bmatrix} \omega_{G_{ss}} \\ \vdots \end{bmatrix}$  $u = \begin{bmatrix} \omega_{ref} \\ P_{L}^{ref} \end{bmatrix}$ 

 $\mathfrak{S}_{PRI}: u[k+1] = u[k] - L_s x_s[k] + L_t x_t[K]$  $\mathfrak{S}_{SEC}: e_s[k+1] = (\tilde{A}_s + C_s E_s)e_s[k] + C_s E_s R_s x_t[K]$ 



### **Transactive Control: Lower Levels**



The overall model, including the primary, secondary, and tertiary level dynamics at multiple time-scales

$$\Sigma_{Pri} : \begin{cases} \dot{x}_{p} = (A + E_{p})x_{p}(t) + Bz_{p}(t) + Fu(k) \\ \epsilon \dot{z}_{p} = Cx_{p}(t) + Dz_{p}(t) + \phi_{p}(t) \end{cases}$$
  

$$\mathscr{I}_{Pri} : u[k+1] = u[k] - L_{s}x_{s}[k] + L_{t}x_{t}[K]$$
  

$$\Sigma_{Sec} : x_{s}[k+1] = (\tilde{A}_{s} + C_{s}E_{s})x_{s}[k] + B_{s}L_{t}x_{t}[K]$$
  

$$\mathscr{I}_{Sec} : e_{s}[k+1] = (\tilde{A}_{s} + C_{s}E_{s})e_{s}[k] + C_{s}E_{s}R_{t}x_{t}[K]$$
  

$$\Sigma_{Ter} : x_{t}[K+1] = \tilde{A}_{t}x_{t}[K] + hk_{\rho}E_{t}e_{s}[K] + b$$



## Transactive Control: Stability\*

If the transactive control is such that

$$Re\left[\lambda_{max}\{A - BC\}\right] < 0 \tag{1a}$$

$$|\lambda_i(\tilde{A}_s)| < 1 \text{ for all } i = 1, \dots n_s \tag{1b}$$

$$|\lambda_i(\tilde{A}_t)| < 1 \text{ for all } i = 1, \dots n_t, \tag{1c}$$

where  $\lambda_i$  is the *i*-th eigenvalue of matrix A and  $\lambda_{max}(A)$  denoted the largest eigenvalue of the matrix A, then there exists  $h^*$ , and  $\epsilon^*$  such that for all  $h \in (0, h^*)$  and  $\epsilon \in (0, \epsilon^*)$ , the equilibrium  $O = (x_{p_{ss}}, x_s^*, e_s^*, x_t^*)$  of the overall hierarchical Transactive control is asymptotically stable.

\* A. Kiani and A.M. Annaswamy, "A Hierarchical Transactive Control Architecture for Renewables Integration in Smart Grids," CDC 2012, Maui, Hawaii.



## Transactive control architecture

The use of dynamic market mechanism to send an incentive signal and receive a feedback signal within the power system's node structure

- Incentive Signal: Ex. Dynamic Pricing
- Feedback Signal:
  - Adjustable Demand (Market Level)
    - (Price Responsive, and Regulation Responsive)
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## Simulation Results

- 4-bus network with two generator units at node 1 and wind at bus 2 (P<sub>g1</sub>: Base-load; P<sub>g2</sub>: Reserve)
- L<sub>1</sub>, L<sub>2</sub>: DR-Compatible demand



Parameters with following values:  $c_{g1} = 0.25$ ;  $c_{g2} = 0.55$ ; generator cost coefficients  $b_{g1} = 40.2$ ;  $b_{g2} = 60$ ; generator cost coefficients  $k_{g1} = 0.3$ ;  $k_{g2} = 0.8$ ; generator time constants  $c_{d1} = c_{d2} = 0.4$ ; consumer utility coefficients  $b_{d1} = b_{d2} = 70$ ; consumer cost coefficients  $k_{d1} = k_{d2} = 0.3$ ; demand time constants k = 0.7; LMP time constant (market time constant)





## Market Stability & Volatility

Volatility: With increased demand-elasticity  $(k_d)$ 

Stability: With increased latency  $(k_{\rho})$ 







#### Simulation Results: Market Stability & Volatility

Volatility: With increased demand-elasticity ( $k_d$ )

Stability: With increased latency  $(k_{\rho})$ 





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## **Simulation Results**

Wind Properties:

- Actual Wind Power
- : Mean value of the projected wind.  $\rightarrow$  Current Market Practice
- : ARMA model of the actual wind power.  $\rightarrow$  With Transactive Control



#### Simulation Results: Effect of Wind Uncertainty



#### Simulation Results: IEEE 30 bus Case





## Summary

- Transactive Control
  - Dynamic Market Mechanisms
  - Integrated Secondary and Primary Control
- Case Studies





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# Thank You!





