

# Anomaly Detection in Premise Energy Consumption Data

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Center)

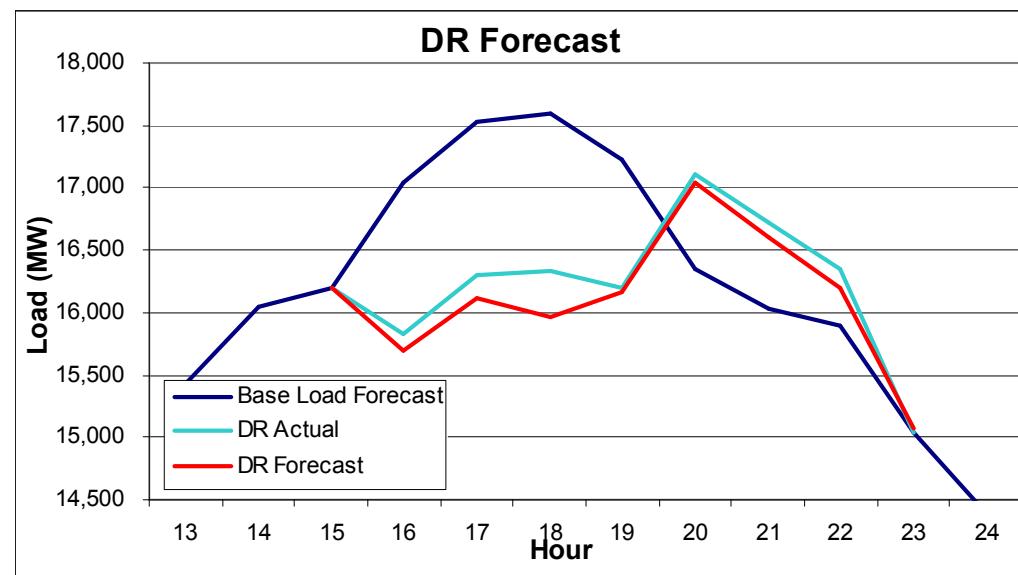
CMU Electricity Conf  
March 2012



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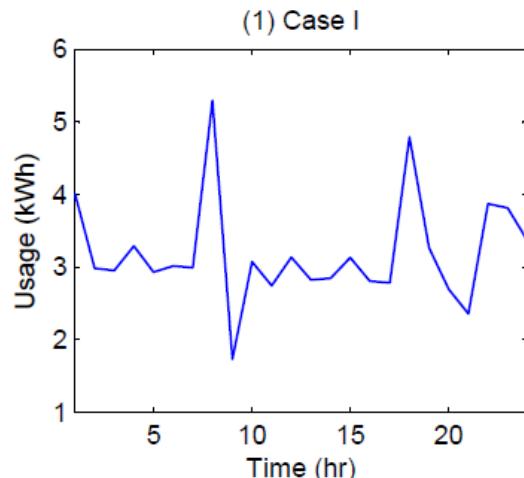
# Demand Response Estimation

- **Critical X's:** weather, Temperature, seasons, days of week, devices, time...
- **X's are gathered from:**
  - AMI data
  - Real time weather forecasts
  - Historical data
- **Methods:**
  - Sampling Methods
  - Categorization Techniques
  - Empirical Methods
  - Regression techniques
  - Bayesian methods
  - Artificial Intelligence – Neural Nets, SVM,...

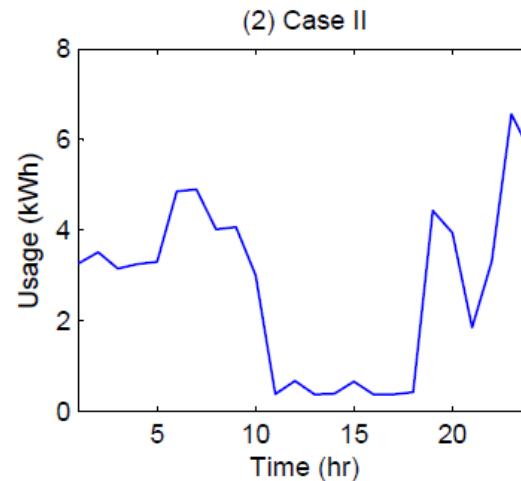


- 2 Error Sources:
  - Base Load Forecast
  - Response Estimate

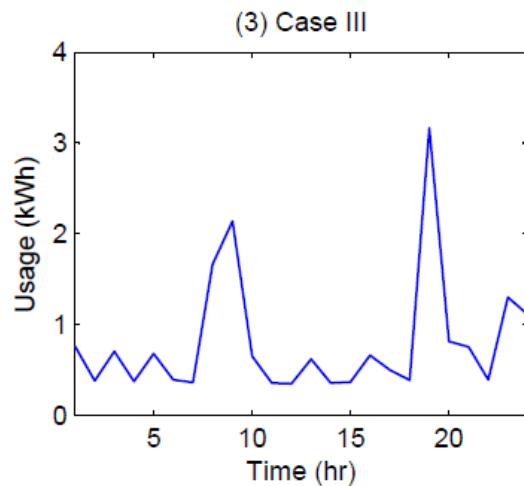
# Typical Household Load Patterns



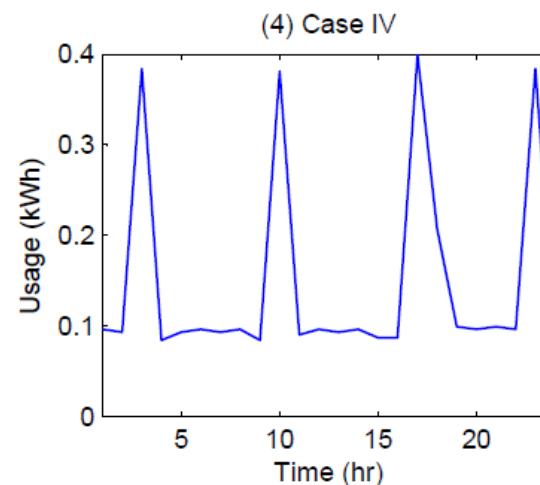
Weekend with heating/AC



Weekday with heating/AC



Weekday without heating/AC



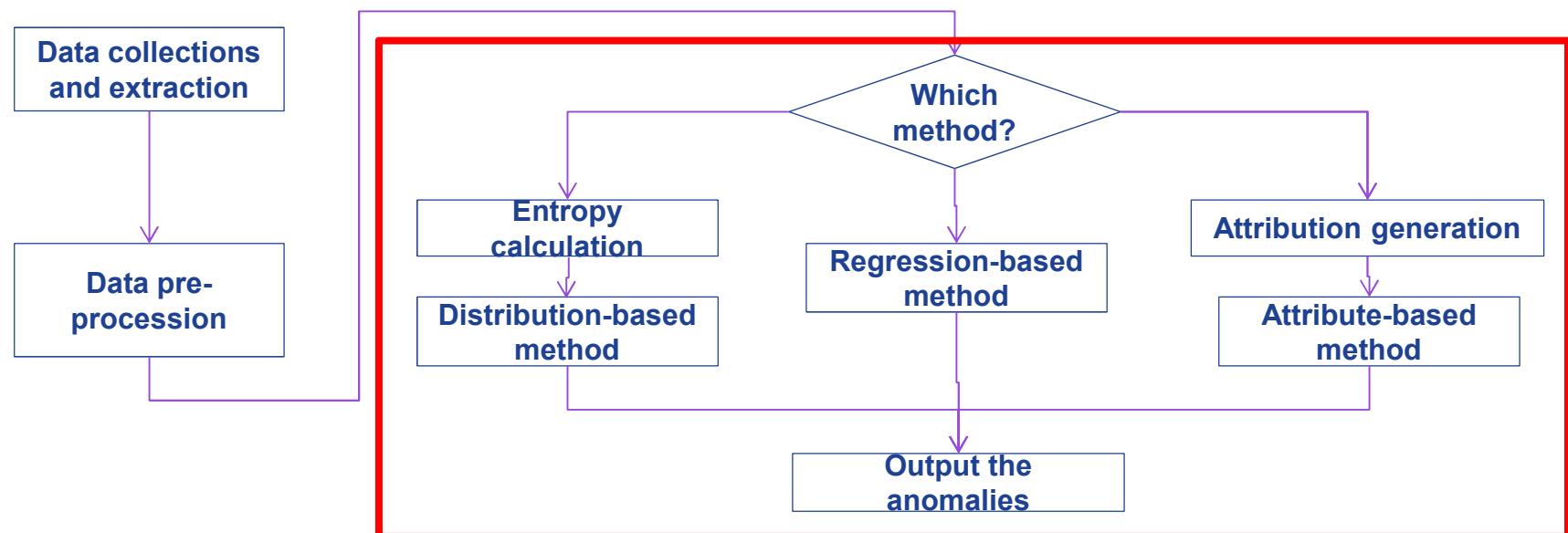
Anomaly



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# Proposed Methods for Anomaly Detection

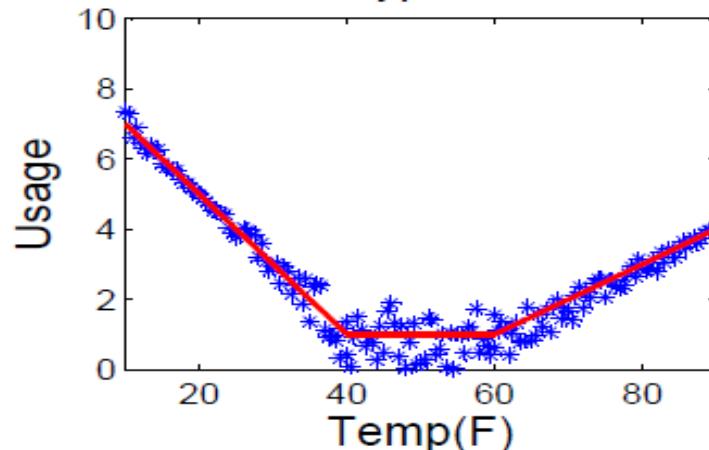
- Regression-Based Anomaly Detection
- Distribution-Based Anomaly Detection
- Attribute-Based Anomaly Detection



# Regression-based Anomaly Detection

## Algorithm:

1. Piecewise regression: 1, 2, and 3 piece linear functions
2. F test: determine the best model  $f(X)$
3. Estimate energy consumption  $\hat{Y} = f(X)$
4. Calculate ratio  $R = \frac{\hat{Y}}{\text{mean } \bar{R}}$ , mean  $\bar{R}$ , and standard



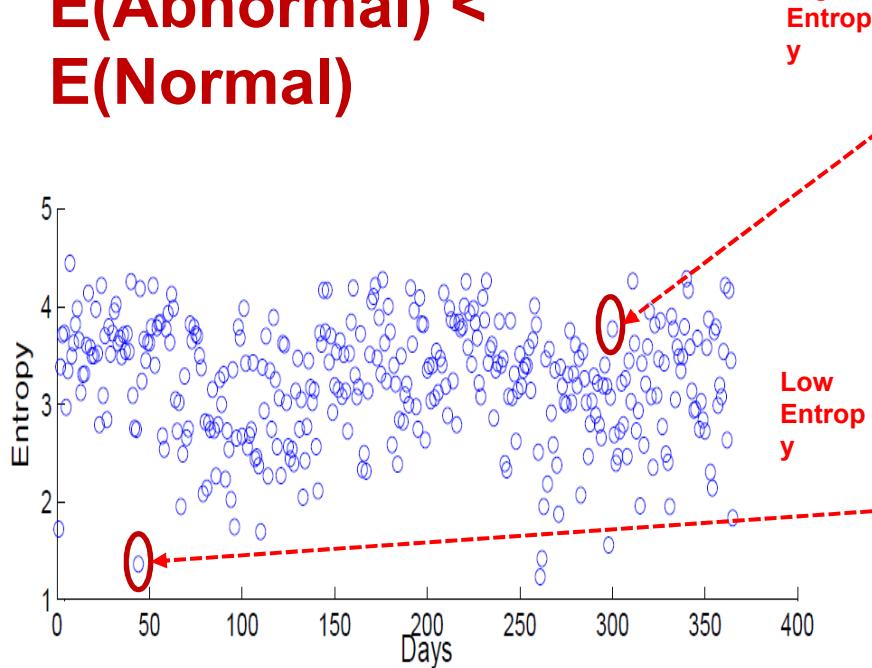
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# Distribution-based Anomaly Detection

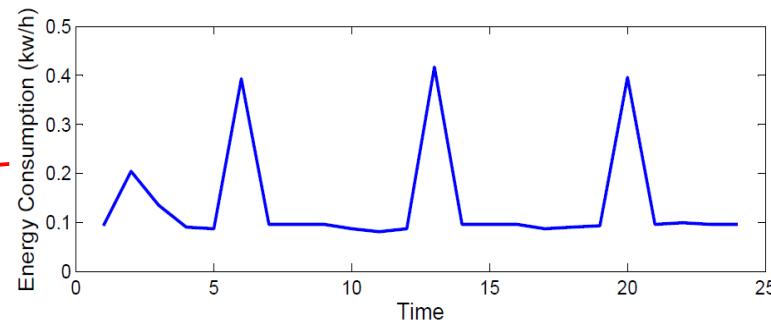
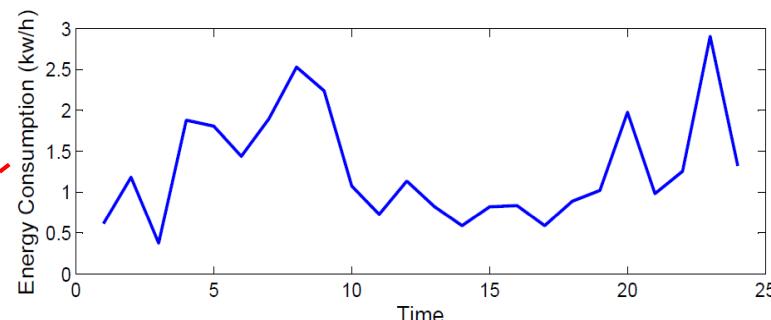
In information theory, entropy is a measure of the uncertainty associated with a random variable.

$$H(x) = \sum_{i=1}^n p(x_i) \log_b p(x_i)$$

**E(Abnormal) < E(Normal)**



**Normal Weekday**



**Abnormal Weekday**

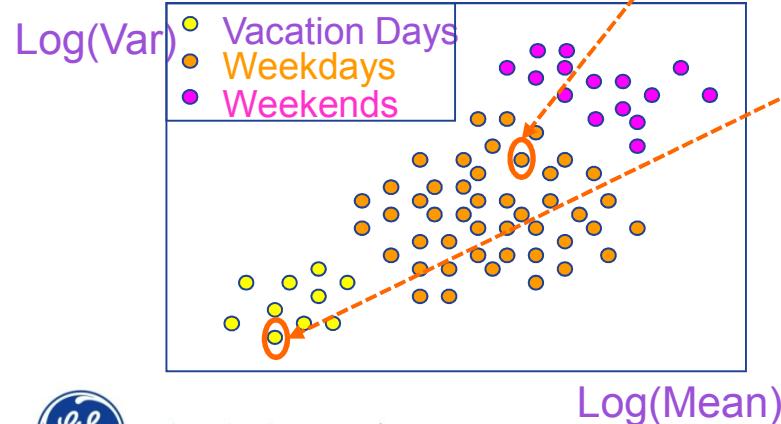


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# Attribute-based Anomaly Detection

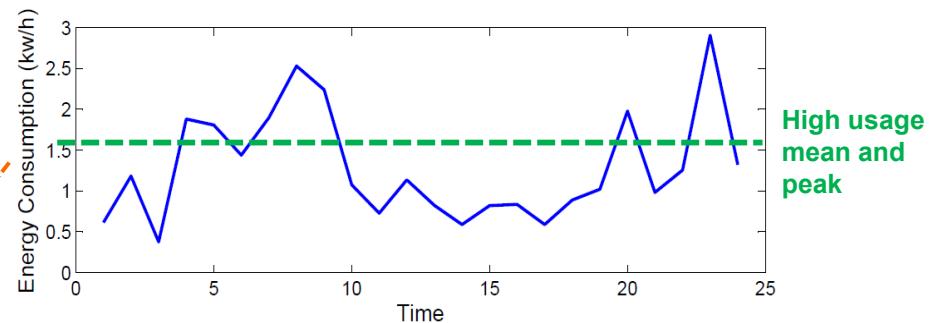
Attributes generated from daily consumption data are:

- mean
- Variance
- Maximum
- range (=maximum - minimum)
- ratio (=maximum/minimum).

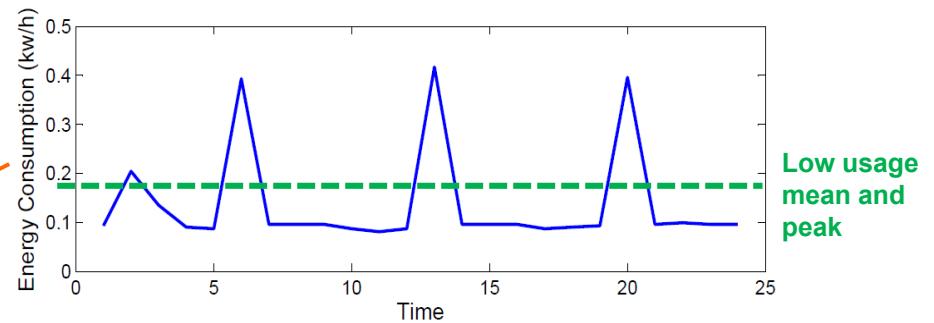


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**Normal Weekday**



**Vacation Weekday**



# Raw Data

## 2 sets of raw data

- Single customer data
- Detailed usage
- 8 months

Time	A/C Down Condensing Unit	A/C Up Condensing Unit	Air Handler Downstairs	Air Handler Upstairs	Computer Room	Dishwasher	Dryer(Gas)	Entertainment Center	Microwave	Other	Range	Pool Pump	Refrigerator	Main	Washer	Indoor Temperature Downstairs	Indoor Temperature Upstairs	Weather Temp
1/1/2010 0:00	0	0	0	0	0.03	0	0	0.01	0	0.01	0	0	0.06	0.1	0	281.97	283.64	53.6
1/1/2010 0:15	0	0	0	0.06	0.03	0	0	0.01	0	0.01	0	0	0.01	0.1	0	282.07	283.53	53.6
1/1/2010 0:30	0	0	0	0	0.03	0	0	0.01	0	0	0	0	0.02	0.05	0	282.01	283.64	53.6
1/1/2010 0:45	0	0	0	0.05	0.03	0	0	0.01	0	0.02	0	0	0.07	0.18	0	282.14	283.71	53.6

- 9-customer data
- Some information is missing
- 90 days

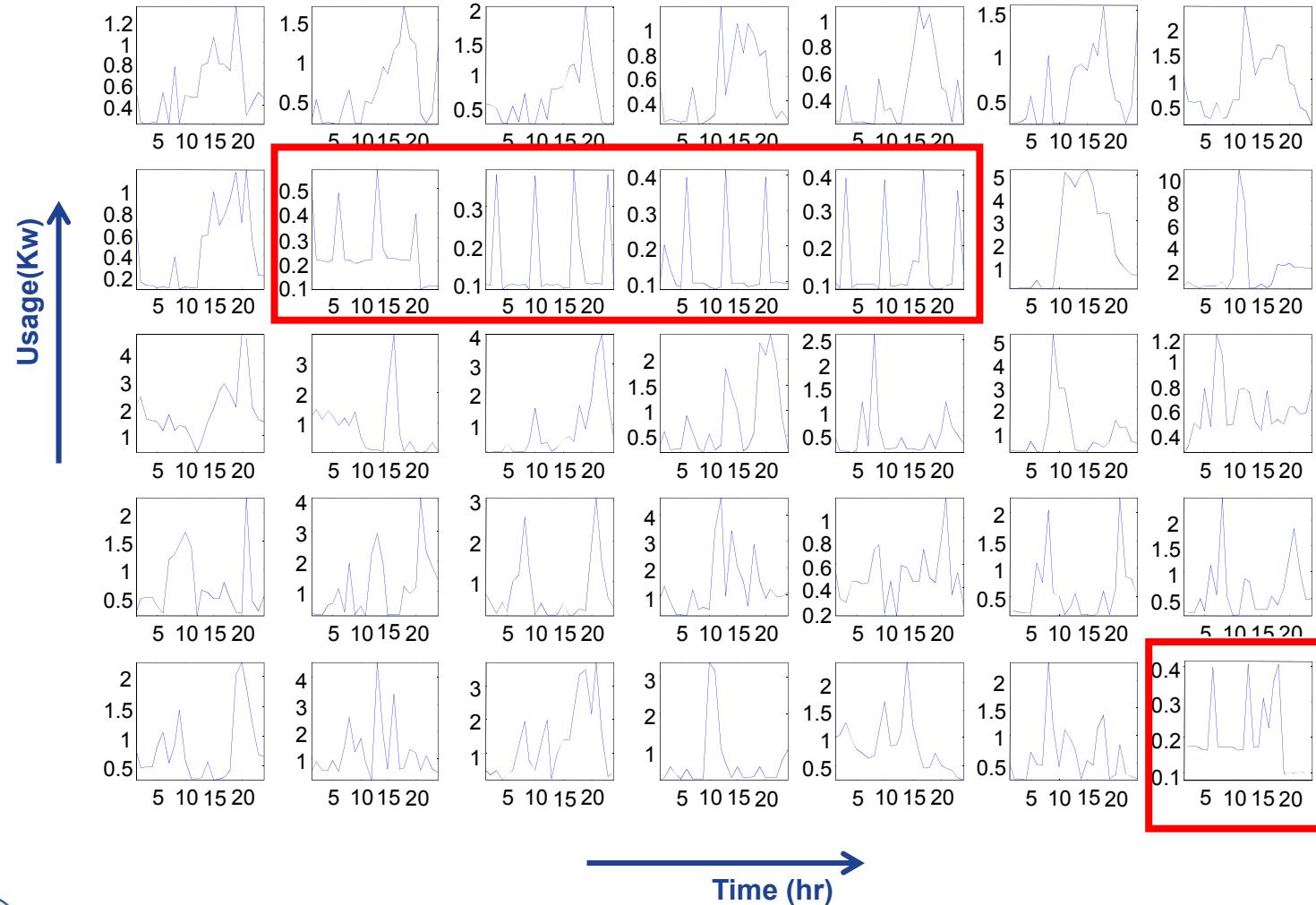
ab	name	'Laurel'		
main		<2160x1 double>	0.0412	1.8768
dryer		<2160x1 double>	0	0.3203
microwave		<2160x1 double>	0	0.5240
range		<2160x1 double>	0	0.5240
refrigerator		<2160x1 double>	0.0053	0.0920
washer		<2160x1 double>	0	0.5240
waterheater		<2160x1 double>	0	0.5240
others		<2160x1 double>	-0.3030	1.4485
ab	time	"		



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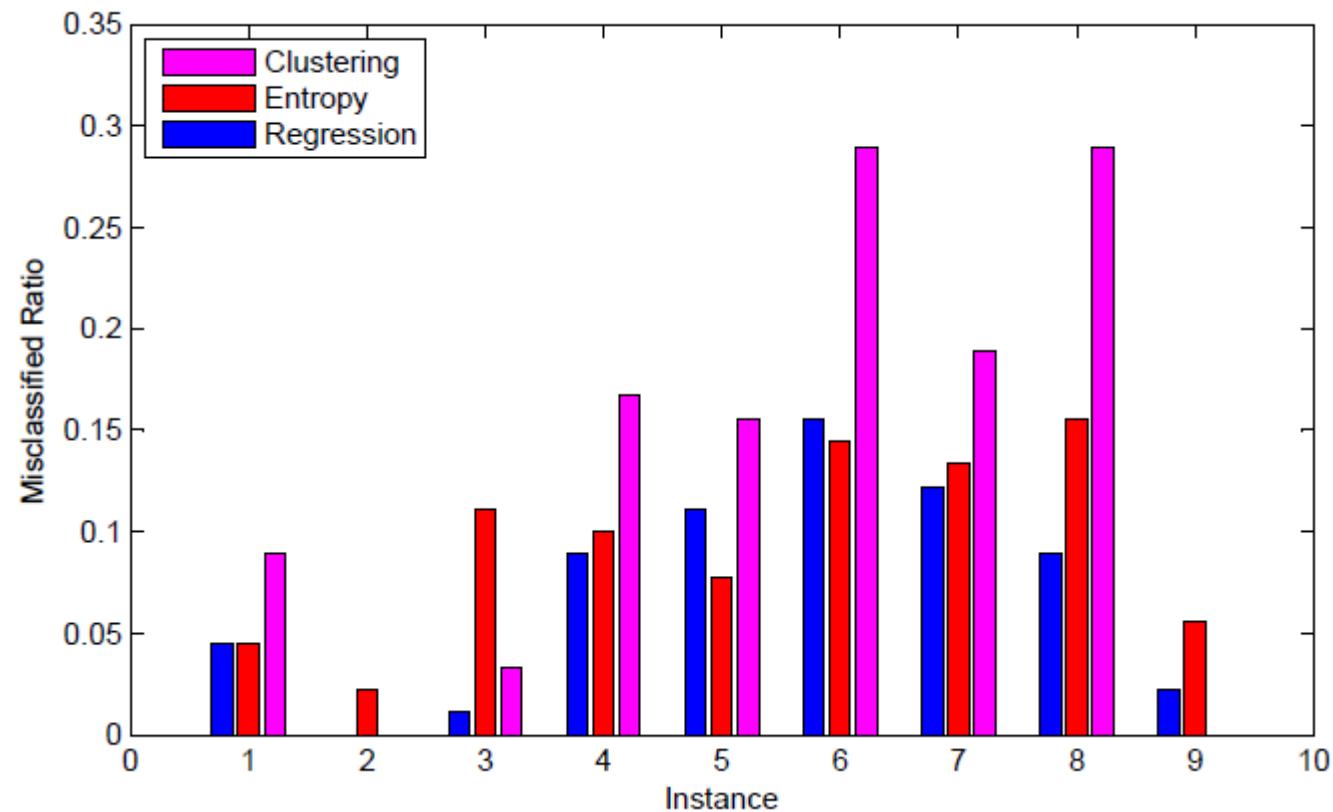
## Abnormal Days Detection

(use statistics, machine learning, etc. to detect days with abnormal behavior/responsiveness  
in nonevent days or during DR events)



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# Simulation Results: 9-customer Data



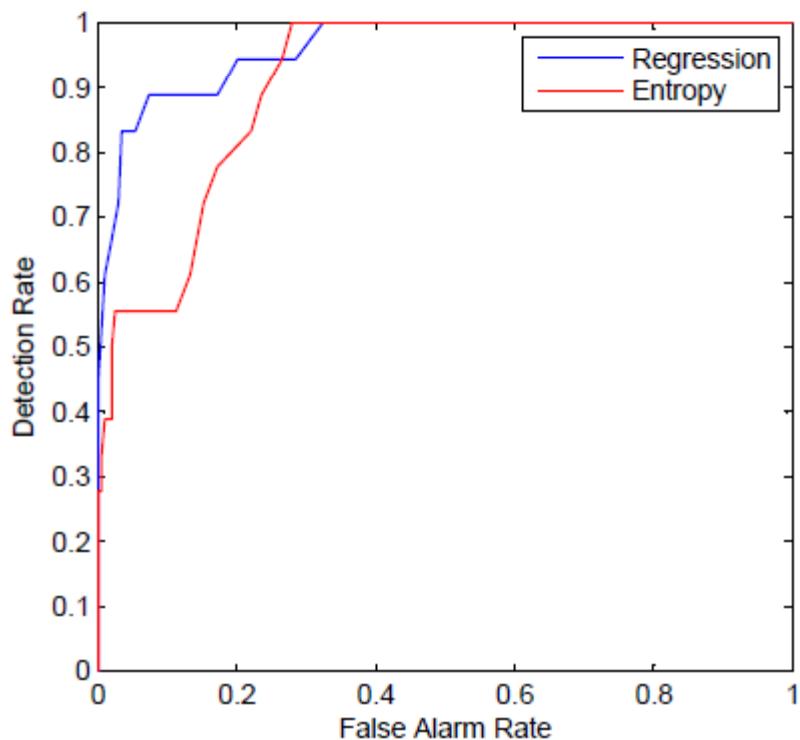
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# Simulation Results: Single-customer Data

## Detection Results

	Detection Rate	False Alarm Rate
Regression	88.89%	7.35%
Entropy	55.56%	9.80%
Clustering	72.22%	30.88%

## ROC Curve



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# Conclusions

- Anomaly detection achievable in demand response estimation.
- Proposed Regression-based, distribution-based, and attribute based methods can be used.
- Data mining on each customer's power consumption profile is required for algorithm selection and parameter tuning



# Backup



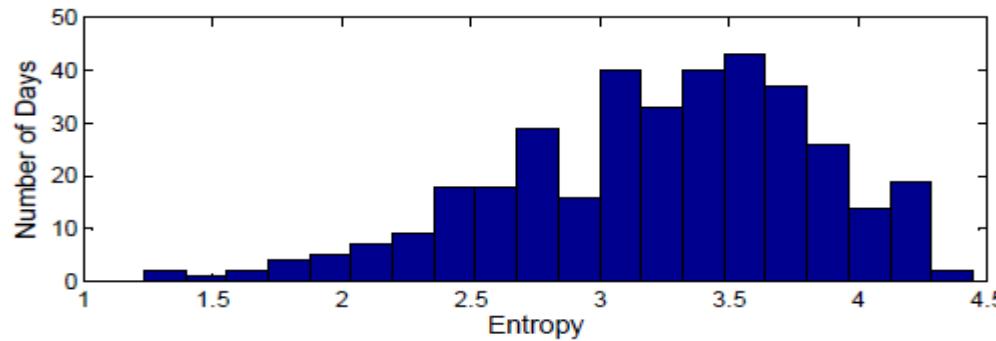
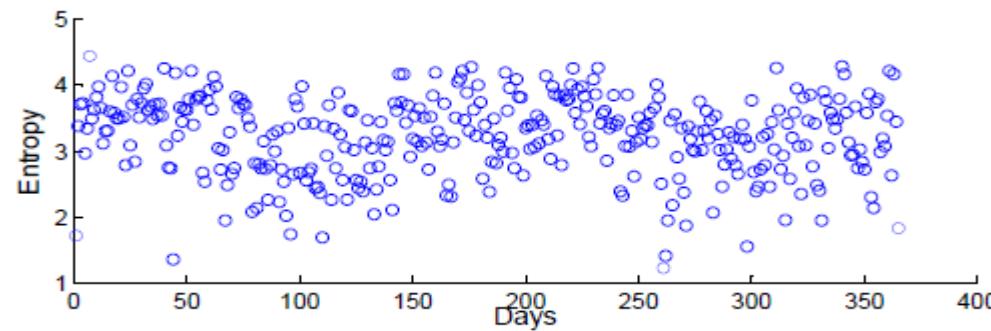
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# Distribution-based Anomaly Detection

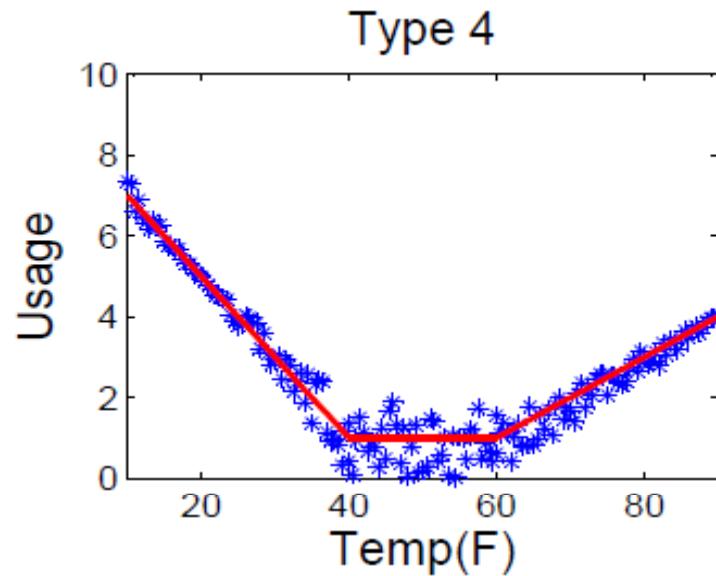
## Algorithm:

1. Normalize energy consumption data
2. Calculate entropy  $H$  for each daily profile, mean  $\bar{H}$ , and standard deviation  $\sigma_H$
3. Identify day  $i$  as an anomaly day if  $H_i < \bar{H} - \alpha \cdot \sigma_H$



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# Piecewise Regression



## 3 Piece Regression

$$y = \begin{cases} a_1x + b_1 & \text{if } x < c_1 \\ a_2x + b_2 & \text{if } c_1 \leq x \leq c_2 \\ a_3x + b_3 & \text{if } x > c_2 \end{cases}$$

$$a_1c_1 + b_1 = a_2c_1 + b_2$$

$$a_2c_2 + b_2 = a_3c_2 + b_3$$



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# Attribute-based Anomaly Detection cont.

## Algorithm:

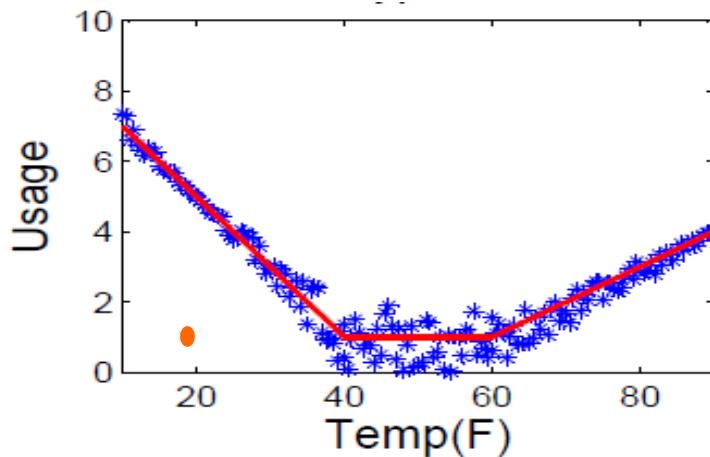
1. Generate attributes from raw energy consumption data
2. Run k-Means clustering n times using random start point and select the best one output
3. Identify the cluster with the smallest mean usage as anomaly days



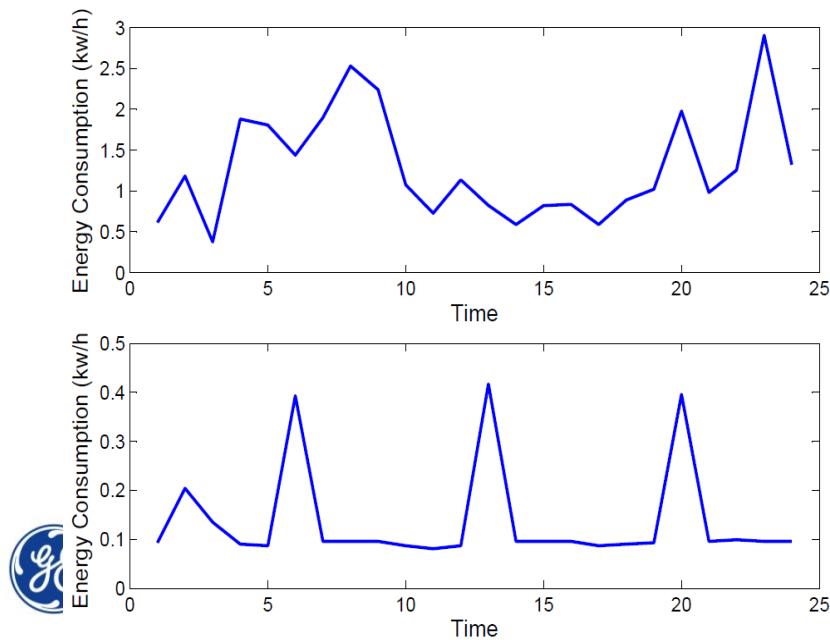
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# Different Anomaly Detection Methodology

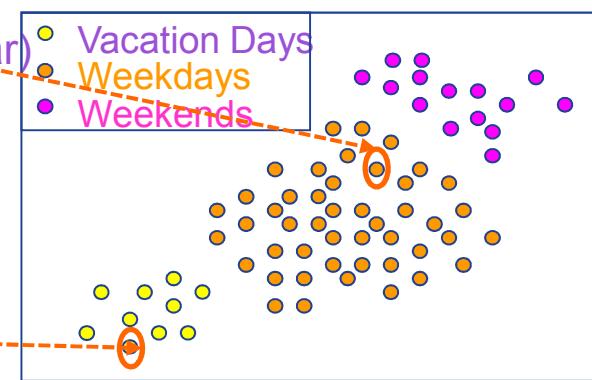
## Regression based



## Distribution based

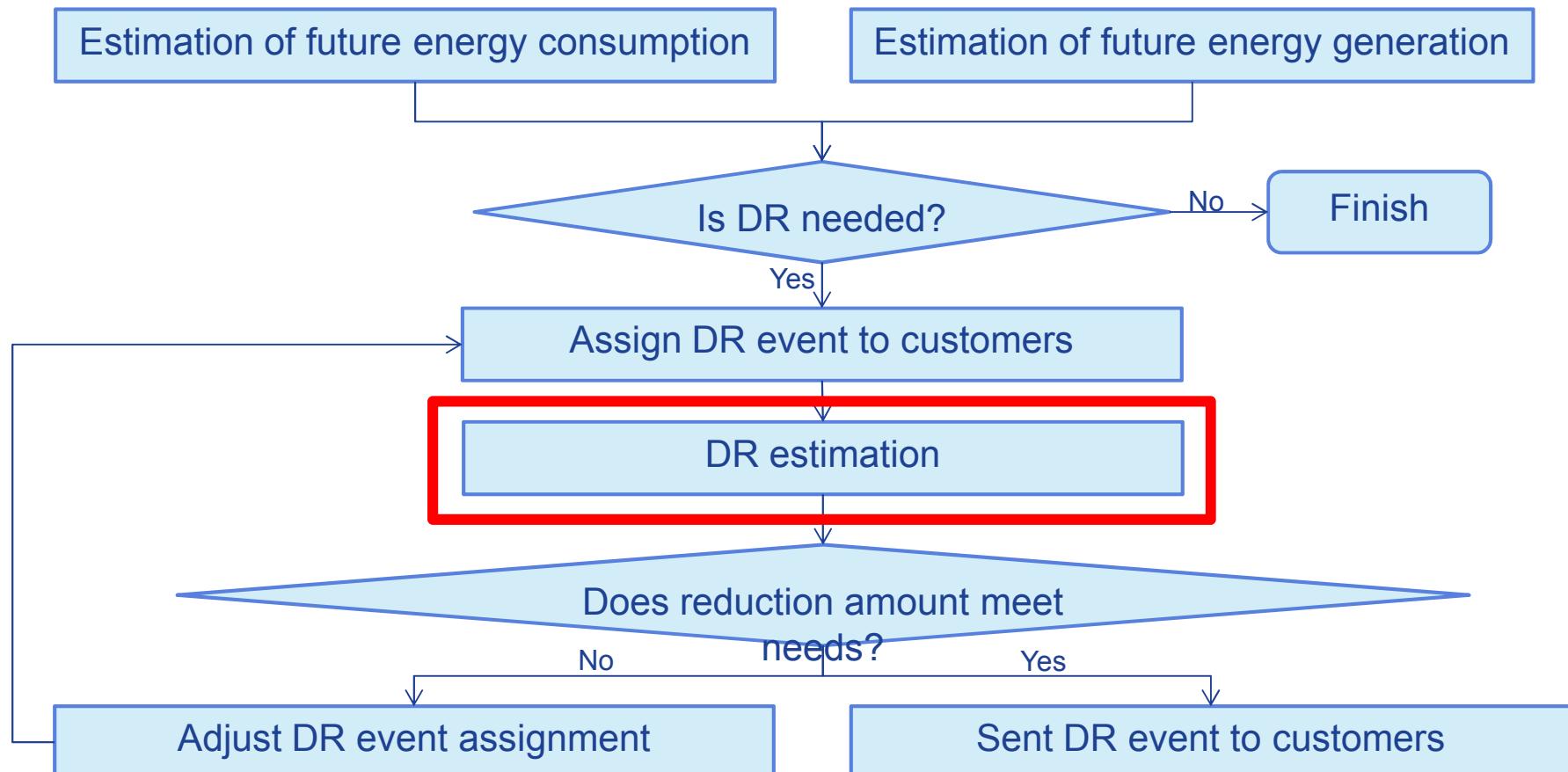


## Attribute based



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# Demand Response (DR) Process



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